

# Crucial Knowledge

A blue trapezoidal box with a slight shadow, containing the text "Year 7".

Year 7

A light green trapezoidal box with a slight shadow, containing the text "Year 8".

Year 8

A purple trapezoidal box with a slight shadow, containing the text "Year 9".

Year 9

# Year 7

Chapter 1

Chapter 2

Chapter 3

Chapter 4

Chapter 5

Chapter 6

Chapter 7

Chapter 8

Chapter 10

Chapter 11

Chapter 15

Chapter 16

Home

# Year 8

Chapter 2

Chapter 3

Chapter 4

Chapter 5

Chapter 6

Chapter 7

Chapter 8

Chapter 10

Chapter 11

Chapter 15

Chapter 16

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# Year 9

Chapter 7

Chapter 2

Chapter 3

Chapter 4

Chapter 5

Chapter 6

Chapter 8

Chapter 11

Chapter 12

Chapter 14

Chapter 15

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# Chapter 1 - Number

## 4 Operators

Addition (or **Sum**) +  
Subtraction (or **Difference**) –  
Multiplication (or **Product**) ×  
Division ÷

## Place Value

- The 'column values' of numbers

....	Thousands	Hundreds	Tens	Units	Decimal Point	$\frac{1}{10}$	$\frac{1}{100}$	$\frac{1}{1000}$	....
------	-----------	----------	------	-------	---------------	----------------	-----------------	------------------	------

## Ordering Decimals

- Set up a table with the decimal point in the same place for each number.
- Put in each number.
- Fill in the empty squares with zeros.
- Compare using the first column on the left.
- If the digits are equal move to the next column to the right until one number is higher.
- This number is the bigger one.

## Multiplying and Dividing by 10, 100, 1000

- When we multiply a number by 10, we move every digit one place value to the left.
- When we multiply a number by 100, we move every digit 2 place values to the left.
- When we multiply a number by 1000, we move every digit 3 places to the left.
- We move each digit the same number of places to the left as there are zeros.
- Remember to fill in any blank spaces with 0 place holders.
- For dividing, we follow the same method but move every digit to the right

## Negative Numbers

+ × + = +	+ ÷ + = +
+ × - = -	+ ÷ - = -
- × + = -	- ÷ + = -
- × - = +	- ÷ - = +

Home

# Chapter 2 - Measures

Length	Area	Capacity and Volume	Mass	Time
1 cm = 10 mm	1 cm <sup>2</sup> = 100 mm <sup>2</sup>	1 cl = 10 ml	1 kg = 1000 g	1 minute = 60 seconds
1 m = 100 cm	1 m <sup>2</sup> = 10 000 cm <sup>2</sup>	1 litre = 100 cl	1 tonne = 1000 kg	1 hour = 60 minutes
1 km = 1000 m	1 ha = 10 000 m <sup>2</sup>	1 litre = 1000 ml		1 day = 24 hours
	1 km <sup>2</sup> = 1 000 000 m <sup>2</sup>	1 litre = 1000 cm <sup>3</sup>		1 week = 7 days
		1 ml = 1 cm <sup>3</sup>		1 year = 365 days

## Area and perimeter

Perimeter is distance around shape

Area is space inside a shape (2D), measure in square units

Rectangle Area = *base x height*

Parallelogram Area = *base x height*

Triangle Area =  $\frac{1}{2} (\text{base} \times \text{height})$

Trapezium Area =  $\frac{1}{2} (a+b) \times \text{height}$

Circle Area =  $\pi \times \text{radius}^2$

Circumference is the perimeter of a circle

Circumference =  $2\pi \times \text{radius}$

## Terminology of Shape

Height – Perpendicular height

Perpendicular – lines meet at 90 degrees

Parallel – always the same distance apart

Edge – Where 2 faces meet on a 3D shape

Vertices – The point where edges meet (corner) on a 3D shape

Face – side of a 3D shape

Quadrilateral – a 4-sided polygon

Polygon – a 2d shape with straight sides

Scalene – all sides and angles are different

Isosceles – 2 sides and angles are the same

Equilateral – 3 sides and angles are the same

Right – contains a right angle

Acute – an angle less than 90°

Obtuse – an angle between 90° and 180°

Reflex – an angle more than 180°

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# Chapter 3 - Expressions

## Algebra terminology

$2y$  is 2 multiplied by the value of 'y'.

So if  $y = 5$  then  $2y = 2 \times 5 = 10$

$y^2$  is the value of 'y' multiplied by itself.

So if  $y = 5$  then  $y^2 = 5 \times 5 = 25$

## Substitution

We can replace letters with numbers to create an answer.

We are normally given a formula and values to put in, but sometimes we have to create the expression and then put values in.

You are told  $E = \frac{1}{2} mv^2$

Calculate E when  $m = 10$  and  $v = 2.5$

$$E = \frac{1}{2} \times 10 \times 2.5^2$$

$$E = 31.25$$

## Simplifying – Collecting like terms

We can only bring 'like terms' together to simplify the expression

Rewrite to get your 'like terms together'

### Adding and Subtracting

$$4a + 3b + 6a - b = 4a + 6a + 3b - b \\ = 10a + 2b$$

$$3f^2 + 5g^2 + 3f^2 - 7g^2 = 3f^2 + 3f^2 + 5g^2 - 7g^2 = \\ 6f^2 - 2g^2$$

### Multiplying and Dividing

$$4a \times 6a = 24a^2$$

(Multiply numbers and add powers)

$$30b^5 \div 5b^2 = 6b^3$$

(Divide numbers and subtract powers)

## Multiplying out single brackets

Bracket create an order (BIDMAS)

Brackets are also an invisible multiply

$$6(a + 3) = 6 \times a + 6 \times 3 = 6a + 18$$

$$5(2b - a) = 5 \times 2b + 5 \times -a = 10b - 5a$$

$$2m(3m - 5) = 2m \times 3m + 2m \times -5 = 6m^2 - 10m$$

# Chapter 4 - FDP

## Fractions

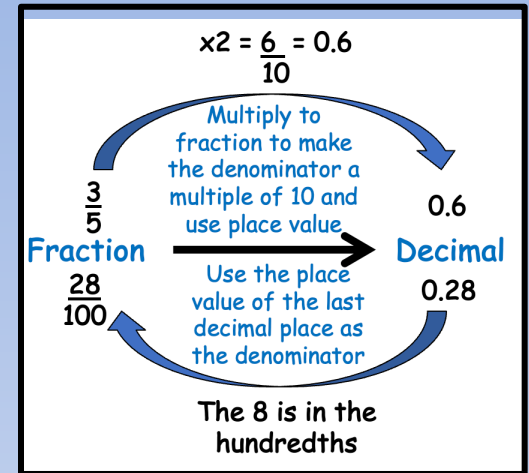
- Bottom term is the denominator
- Top term is the numerator

## Fractions of a quantity

- Divide by the denominator
- Multiply by the numerator

## Simplifying Fractions

Divide the numerator and denominator by their highest common factor.



## Fraction Arithmetic

**Multiplying** – Multiply top by top and bottom by bottom.

**Dividing** - 'Keep Change Flip'.

**Addition or Subtraction** –

You need same bottom number (**denominator**). Add or subtract the numerator, keep the denominator the same.

## Percentages

- An amount out of 100

- **With a calculator:**

What is 40% of £50

**Percentage  $\div 100 \times$  amount**

- **Changing to a percentage:**

**Amount  $\div$  total  $\times 100$**

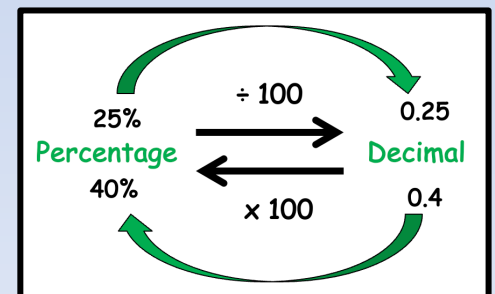
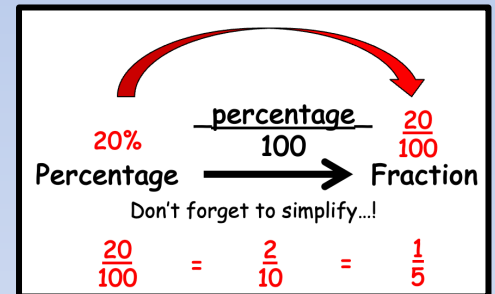
- **Without a calculator:**

**1% = divide by 100**

**10% = divide by 10**

**25% = divide by 4**

**50% = divide by 2**



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# Chapter 5 – Angles and 2D Shapes

## Use of Protractor

- Estimate the size of the angle
- Line up the cross with the origin of the angle
- Rotate the protractor to align the baseline of the angle with the protractor
- Follow the upper line of the angle and measure on the protractor's arc to read the degrees

## Angle Reasoning

Angles on straight line =  $180^\circ$

Angles in a triangle =  $180^\circ$

Angles in quadrilateral =  $360^\circ$

Angles at a point =  $360^\circ$

## Angles with parallel lines

Vertically opposite angles are always equal

F – Corresponding angles are always equal

Z – Alternate angles are always equal

C – Co-Interior always add to 180

## Polygons

A shape with 3 or more straight sides

Total Interior Angles =  $(n-2) \times 180$

Interior + Exterior =  $180^\circ$

Sum of Exterior =  $360^\circ$

# Chapter 6 - Graphs

## Coordinates

Remember “along the corridor then up the stairs”  
X and y values should be written on the axes  
There are 4 quadrants

## Horizontal and Vertical Lines

- An equation in the form  $y =$  always gives a horizontal line.
- An equation in the form  $x =$  always gives a vertical line.

## Parallel lines

- Parallel lines have the same gradient

## Plotting Straight Lines

- When plotting a linear graph always plot at least three coordinates.
- First create a table of values
- Substitute in values to form coordinate points
- Plot the coordinates one at a time

# Chapter 7 - Calculations

## BIDMAS

The **order** you do calculations in:

**B** rackets

**I** ndices

**D** ivision

**M** ultiplication

**A** ddition

**S** ubtraction

## Rounding

Decimal places (column after decimal point)

Significant Figures (highest value column)

## Negative Numbers

$$+ \times + = + \quad + \div + = +$$

$$+ \times - = - \quad + \div - = -$$

$$- \times + = - \quad - \div + = -$$

$$- \times - = + \quad - \div - = +$$

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# Chapter 8 - Statistics

## Mean, median, mode and range

You must be able to get measures from a list of values or values in a frequency table

**MEAN** = Total of values  $\div$  Number of values

**MEDIAN** – The middle value when written in size order

**MODE** – The value that occurs the most often

**RANGE** – Maximum value – Minimum value

### Displaying data

Bar Chart



Pie Chart



Pictogram

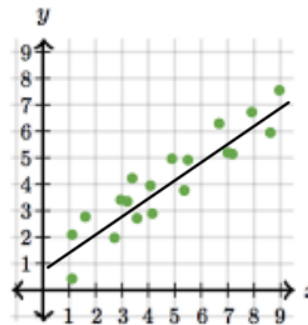
Car	   
Bus	  
Lorry	 
Bike	  
Van	 

Stem and Leaf

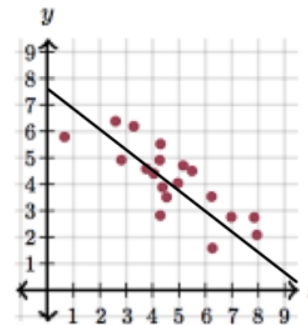
Stem	Leaf
1	2 3
2	1 7
3	3 4 5 7 7
4	0 0 1

### Interpreting data

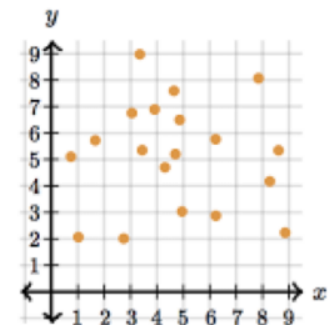
- Get values from bar charts
- Get values from pie Charts
- Use key to get values from Stem and Leaf diagram
- Use key to get values from Pictogram



Positive Correlation



Negative Correlation



No Correlation

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# Chapter 10 - Equations

## Solving equations

- To get a numerical answer for a letter
- We have to do the same to both sides of the equals sign
- If we move things across the equals sign we use the opposite operation

$$\text{Solve } 4y + 1 = 17$$

Move +1 over to become -1

$$4y = 17 - 1 \text{ so } 4y = 16$$

Move  $\times 4$  over to become  $\div 4$  so  $y = 16 \div 4$

$$\underline{y = 4}$$

$$\text{Solve } 2(3y + 1) = 20$$

Expand bracket

$$2 \times 3y = 6y \text{ and } 2 \times 1 = 2 \text{ so}$$

$$6y + 2 = 20 \text{ Move } +2 \text{ over to become } -2$$

$$6y = 20 - 2 \text{ so } 6y = 18$$

Move  $\times 6$  over to become  $\div 6$  so  $y = 18 \div 6$

$$\underline{y = 3}$$

# Chapter 11 – Powers and Roots

## Factors and Multiples

- A factor divides into a number without leaving any remainder
- A multiple of a number is any number in its times table

## Prime Numbers

Have **exactly two factors**

No other whole numbers, except **1** and **itself** divide into them

## Highest Common Factor (HCF)

Write down all the factors from the numbers and find the biggest value on both lists – This is the **Highest Common Factor**

## Lowest Common Multiple (LCM)

Write down all the multiples of the two numbers and find the smallest on both lists – This is the **Lowest Common Multiple**

# Chapter 15 – Ratio and Proportion

## Ratio as a measure

A ratio is a comparison of parts

Use a colon (:) to separate parts of a ratio

A colon is read as 'to'

2 or 3 parts

Understand the parts add up and stay in proportion

## Cancelling ratios

Like simplifying fractions

Look for common factors

Do the same to both parts of the ratio

**3:6**

÷3    ÷3

**1:2**

## Equivalent ratios

Same values but different numbers

Values used can get larger, as well as smaller

Do same to all parts

**3:6**

x4    x4

**12:24**

## Dividing a given ratio

The question matches the order of items to the order of parts in the ratio. The first thing mentioned gets the first part of the ratio

Find the total number of parts in the ratio (+)

Divide the amount to be shared by the total parts (÷)

Multiply by each part of the ratio (x)

### Example

**Q: Adam and Ben share £45 in the ratio 1:2. Who gets how much?**

**A:**            **1 + 2 = 3** parts in total

**£45 ÷ 3 = £15** per part

**1:2**

**x15    x15**

**15:30**

**Adam gets £15 and Ben gets £30**

# Chapter 16 - Probability

## Probability definition and scale

Outcome – A possible result of an experiment

Event – A set of outcomes

Impossible – An outcome that cannot happen

Certain – An event that must happen

## Sample space diagrams

- A list of all possible outcomes from an event.
- We use this to help calculate probabilities

## Probability and relative frequency

A list of all probabilities adds up to 1

Relative frequency =  $\frac{\textit{Times occured}}{\textit{Number of trials}}$

# Chapter 2 - Measures

Length	Area	Capacity and Volume	Mass	Time
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## Area and perimeter

Perimeter is distance around shape

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Obtuse – an angle between 90° and 180°

Reflex – an angle more than 180°

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# Chapter 3 - Expressions

## Simplifying – Collecting like terms

We can only bring 'like terms' together to simplify the expression

Rewrite to get your 'like terms together'

### Adding and Subtracting

$$4a + 3b + 6a - b = 4a + 6a + 3b - b \\ = 10a + 2b$$

$$3f^2 + 5g^2 + 3f^2 - 7g^2 = 3f^2 + 3f^2 + 5g^2 - 7g^2 \\ = 6f^2 - 2g^2$$

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(Multiply numbers and add powers)

$$30b^5 \div 5b^2 = 6b^3$$

(Divide numbers and subtract powers)

## Multiplying out single brackets

Bracket create an order (BIDMAS)

Brackets are also an invisible multiply

$$6(a + 3) = 6 \times a + 6 \times 3 = 6a + 18$$

$$5(2b - a) = 5 \times 2b + 5 \times -a = 10b - 5a$$

$$2m(3m - 5) = 2m \times 3m + 2m \times -5 = 6m^2 - 10m$$

## Substitution

We can replace letters with numbers to create an answer. We are normally given a formula and values to put in, but sometimes we have to create the expression and then

put values in. You are told  $E = \frac{1}{2}mv^2$

Calculate E when  $m = 10$  and  $v = 2.5$

$$E = \frac{1}{2} \times 10 \times 2.5^2$$

$$E = 31.25$$

## Powers

If we multiply powers we add.  $y^3 \times y^4 = y^{(3+4)} = y^7$

If we divide powers we subtract.  $y^{10} \div y^6 = y^{(10-6)} = y^4$

Anything to the power zero is always 1

Home

# Chapter 4 - FDP

## Fractions

- Bottom term is the denominator
- Top term is the numerator

## Fractions of a quantity

- Divide by the denominator
- Multiply by the numerator

## Fraction Arithmetic

**Multiplying** – Multiply top by top and bottom by bottom.

**Dividing** - 'Keep Change Flip'.

**Addition or Subtraction** – You need same bottom number (denominator). Add or subtract the numerator, keep the denominator the same.

## Percentages

- An amount out of 100

- **With a calculator:**

What is 40% of £50

**Percentage  $\div$  100  $\times$  amount**

- **Changing to a percentage:**

**Amount  $\div$  total  $\times$  100**

- **Without a calculator:**

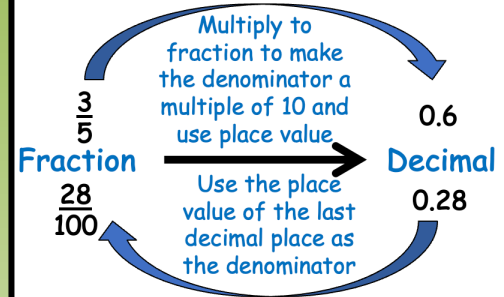
**1% = divide by 100**

**10% = divide by 10**

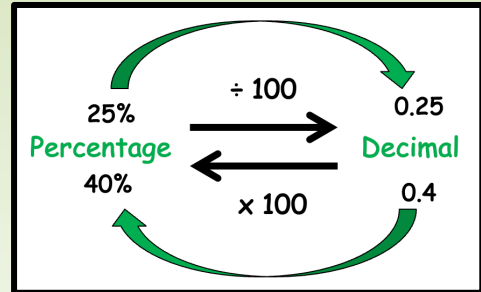
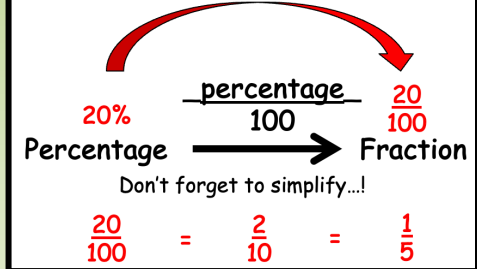
**25% = divide by 4**

**50% = divide by 2**

$$\times 2 = \frac{6}{10} = 0.6$$



The 8 is in the hundredths



## Improper and Mixed Fractions

**Improper to mixed:**

$$2\frac{3}{4} = \frac{(4 \times 2) + 3}{4} = \frac{11}{4}$$

**Mixed fractions to improper**

$$\frac{5}{3} = 5 \div 3 = 1 \text{ R}2$$

$$1\frac{2}{3}$$

Home

# Chapter 5 – Angles and 2D Shapes

## Polygons

A shape with 3 or more straight sides

Total Interior Angles =  $(n-2) \times 180$

Interior + Exterior =  $180^\circ$

Sum of Exterior =  $360^\circ$

## Angles with parallel lines

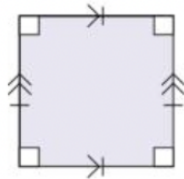
Vertically opposite angles are always equal

F – Corresponding angles are always equal

Z – Alternate angles are always equal

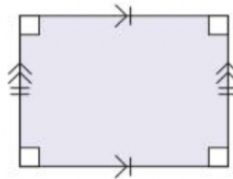
C – Co-Interior always add to 180

**Square**



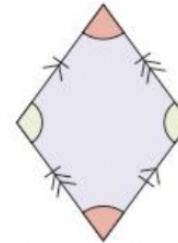
4 equal sides  
4 angles of  $90^\circ$   
2 sets of parallel sides

**Rectangle**



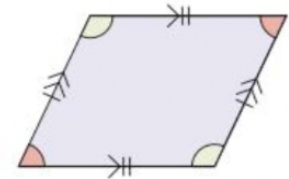
2 sets of equal sides  
4 angles of  $90^\circ$   
2 sets of parallel sides

**Rhombus**



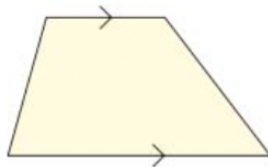
4 equal sides  
2 pairs of equal angles  
2 sets of parallel sides

**Parallelogram**



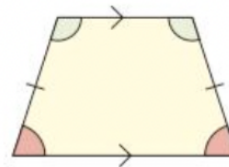
2 sets of equal sides  
2 pairs of equal angles  
2 sets of parallel sides

**Trapezium**



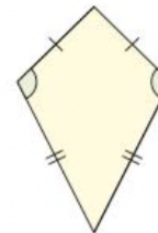
1 set of parallel sides

**Isosceles trapezium**



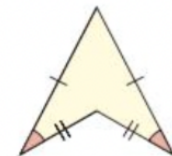
1 set of equal sides  
2 pairs of equal angles  
1 set of parallel sides

**Kite**



2 sets of equal sides  
1 pair of equal angles  
No parallel sides

**Arrowhead**



2 sets of equal sides  
1 pair of equal angles  
No parallel sides

Home

# Chapter 6 - Graphs

## Coordinates

Remember “along the corridor then up the stairs”  
X and y values should be written on the axes  
There are 4 quadrants

## Horizontal and Vertical Lines

- An equation in the form  $y =$  always gives a horizontal line.
- An equation in the form  $x =$  always gives a vertical line.

## Parallel lines

- Parallel lines have the same gradient

## Plotting Straight Lines

- When plotting a linear graph always plot at least three coordinates.
- First create a table of values
- Substitute in values to form coordinate points
- Plot the coordinates one at a time

# Chapter 7 - Calculations

## Getting to Know Your Calculator

$x^2$	Squared (e.g. $3^2 = 3 \times 3 = 9$ )
SHIFT	Gets the second function of the key
$\sqrt{\quad}$	Square Root (e.g. $\sqrt{9} = 3$ )
S $\leftrightarrow$ D	Changes a fraction answer to a decimal
$x^3$	Cubed (e.g. $2^3 = 2 \times 2 \times 2 = 8$ )
"(" and ")"	Brackets
$\sqrt[3]{\quad}$	Cube Root (e.g. $\sqrt[3]{8} = 2$ )
$\frac{\square}{\square}$	Fraction

## Adding & Subtracting Decimals

Use the column method

Line up the decimal places

## Multiplying Decimals

Ignore the decimal place and multiply the digits

Count how many numbers are after the decimal place in the question.

Make sure the answer has the same number

## Dividing Decimals

Multiply both numbers by 10 or 100 to get the numbers from a decimal to a whole number.

Divide using the bus stop method

## Negative Numbers

$$+ \times + = + \quad + \div + = +$$

$$+ \times - = - \quad + \div - = -$$

$$- \times + = - \quad - \div + = -$$

$$- \times - = + \quad - \div - = +$$

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# Chapter 8 - Statistics

## Mean, median, mode and range

You must be able to get measures from a list of values or values in a frequency table

**MEAN** = Total of values  $\div$  Number of values

**MEDIAN** – The middle value when written in size order

**MODE** – The value that occurs the most often

**RANGE** – Maximum value – Minimum value

## Displaying data

Bar Chart



Pie Chart

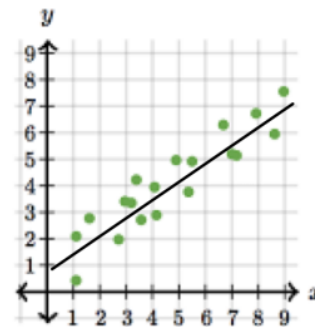


Pictogram

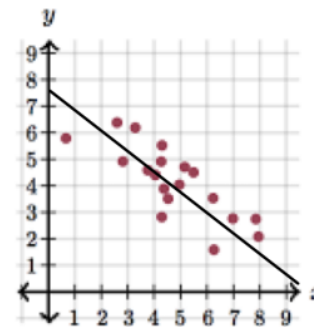
Car	   
Bus	  
Lorry	 
Bike	  
Van	 

Stem and Leaf

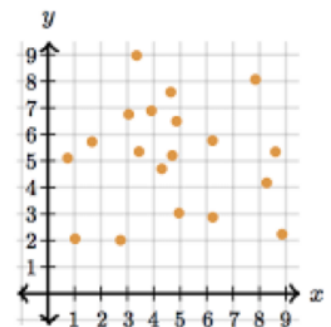
Stem	Leaf
1	2 3
2	1 7
3	3 4 5 7 7
4	0 0 1



Positive Correlation



Negative Correlation



No Correlation

# Chapter 10 - Equations

## Solving equations

- To get a numerical answer for a letter
- We have to do the same to both sides of the equals sign
- If we move things across the equals sign we use the opposite operation

$$\text{Solve } 4y + 1 = 17$$

Move +1 over to become -1

$$4y = 17 - 1 \text{ so } 4y = 16$$

Move x4 over to become  $\div 4$  so  $y = 16 \div 4$

$$\underline{y = 4}$$

$$\text{Solve } 2(3y + 1) = 20$$

Expand bracket

$$2 \times 3y = 6y \text{ and } 2 \times 1 = 2 \text{ so}$$

$$6y + 2 = 20 \text{ Move } +2 \text{ over to become } -2$$

$$6y = 20 - 2 \text{ so } 6y = 18$$

Move x6 over to become  $\div 6$  so  $y = 18 \div 6$

$$\underline{y = 3}$$

# Chapter 11 – Powers and Roots

[Home](#)

# Chapter 15 – Ratio and Proportion

## Ratio as a measure

A ratio is a comparison of parts

Use a colon (:) to separate parts of a ratio

A colon is read as 'to'

2 or 3 parts

Understand the parts add up and stay in proportion

## Recipe Scaling

Work out we have enough to complete

How much of something do we need

**Example:**

**Q: A recipe uses 300g of flour and 150g of butter to make a cake for 4 people. How much of each ingredient is needed to bake a cake for 6 people.**

**A:  $6 \div 4 = 1.5$  (scale factor).**

**$300\text{g} \times 1.5 = 450\text{g}$  flour**

**$150 \times 1.5 = 225\text{g}$  butter**

## Dividing a given ratio

The question matches the order of items to the order of parts in the ratio. The first thing mentioned gets the first part of the ratio

Find the total number of parts in the ratio (+)

Divide the amount to be shared by the total parts ( $\div$ )

Multiply by each part of the ratio ( $\times$ )

**Example**

**Q: Adam and Ben share £45 in the ratio 1:2. Who gets how much?**

**A:  $1 + 2 = 3$  parts in total**

**$\pounds 45 \div 3 = \pounds 15$  per part**

**1:2**

**$\times 15 \quad \times 15$**

**15:30**

**Adam gets £15 and Ben gets £30**

# Chapter 16 - Probability

## Probability definition and scale

Outcome – A possible result of an experiment

Event – A set of outcomes

Impossible – An outcome that cannot happen

Certain – An event that must happen

## Sample space diagrams

- A list of all possible outcomes from an event.
- We use this to help calculate probabilities

## Probability and relative frequency

A list of all probabilities adds up to 1

Relative frequency =  $\frac{\textit{Times occurred}}{\textit{Number of trials}}$

## Probability trees

- Used to show outcomes of multiple events
- All branches add up to 1
- Multiply along branches to find probabilities
- Add multiple routes through tree

# Chapter 7 - Calculations

## Getting to Know Your Calculator

$x^2$	Squared (e.g. $3^2 = 3 \times 3 = 9$ )
SHIFT	Gets the second function of the key
$\sqrt{\quad}$	Square Root (e.g. $\sqrt{9} = 3$ )
S $\leftrightarrow$ D	Changes a fraction answer to a decimal
$x^3$	Cubed (e.g. $2^3 = 2 \times 2 \times 2 = 8$ )
"(" and ")"	Brackets
$\sqrt[3]{\quad}$	Cube Root (e.g. $\sqrt[3]{8} = 2$ )
$\frac{\square}{\square}$	Fraction

## Adding & Subtracting Decimals

Use the column method

Line up the decimal places

## Multiplying Decimals

Ignore the decimal place and multiply the digits

Count how many numbers are after the decimal place in the question.

Make sure the answer has the same number

## Dividing Decimals

Multiply both numbers by 10 or 100 to get the numbers from a decimal to a whole number.

Divide using the bus stop method

## Negative Numbers

$$+ \times + = + \quad + \div + = +$$

$$+ \times - = - \quad + \div - = -$$

$$- \times + = - \quad - \div + = -$$

$$- \times - = + \quad - \div - = +$$

# Chapter 2 - Measures

Length	Area	Capacity and Volume	Mass	Time
1 cm = 10 mm	1 cm <sup>2</sup> = 100 mm <sup>2</sup>	1 cl = 10 ml	1 kg = 1000 g	1 minute = 60 seconds
1 m = 100 cm	1 m <sup>2</sup> = 10 000 cm <sup>2</sup>	1 litre = 100 cl	1 tonne = 1000 kg	1 hour = 60 minutes
1 km = 1000 m	1 ha = 10 000 m <sup>2</sup>	1 litre = 1000 ml		1 day = 24 hours
	1 km <sup>2</sup> = 1 000 000 m <sup>2</sup>	1 litre = 1000 cm <sup>3</sup>		1 week = 7 days
		1 ml = 1 cm <sup>3</sup>		1 year = 365 days

## Area and perimeter

Perimeter is distance around shape

Area is space inside a shape (2D), measure in square units

Rectangle Area = *base x height*

Parallelogram Area = *base x height*

Triangle = Area =  $\frac{1}{2} (\text{base} \times \text{height})$

Trapezium Area =  $\frac{1}{2} (a+b) \times \text{height}$

Circle Area =  $\pi \times \text{radius}^2$

Circumference is the perimeter of a circle

Circumference =  $2\pi \times \text{radius}$

## Terminology of Shape

Height – Perpendicular height

Perpendicular – lines meet at 90 degrees

Parallel – always the same distance apart

Edge – Where 2 faces meet on a 3D shape

Vertices – The point where edges meet (corner) on a 3D shape

Face – side of a 3D shape

Quadrilateral – a 4-sided polygon

Polygon – a 2d shape with straight sides

Scalene – all sides and angles are different

Isosceles – 2 sides and angles are the same

Equilateral – 3 sides and angles are the same

Right – contains a right angle

Acute – an angle less than 90°

Obtuse – an angle between 90° and 180°

Reflex – an angle more than 180°

# Chapter 3 - Expressions

## Multiplying out single brackets

Bracket create an order (BIDMAS)

Brackets are also an invisible multiply

$$6(a + 3) = 6 \times a + 6 \times 3 = 6a + 18$$

$$5(2b - a) = 5 \times 2b + 5 \times -a = 10b - 5a$$

$$2m(3m - 5) = 2m \times 3m + 2m \times -5 = 6m^2 - 10m$$

## Powers

If we multiply the powers, we add.

$$y^3 \times y^4 = y^{(3+4)} = y^7$$

If we divide the powers, we subtract.

$$y^{10} \div y^6 = y^{(10-6)} = y^4$$

Anything to the power zero is always 1

## Substitution

We can replace letters with numbers to create an answer. We are normally given a formula and values to put in, but sometimes we have to create the expression and then put values

in. You are told  $E = \frac{1}{2}mv^2$

Calculate E when  $m = 10$  and  $v = 2.5$

$$E = \frac{1}{2} \times 10 \times 2.5^2$$

$$E = 31.25$$

## Factorising

The process of putting things into brackets

**Factorise  $10a + 5b$**

The highest common factor of  $10a$  and  $5b$  is 5

$2a + b$  in brackets because when these are multiplied by 5 you get your  $10a$  and  $5b$

$5(2a + b)$  is answer

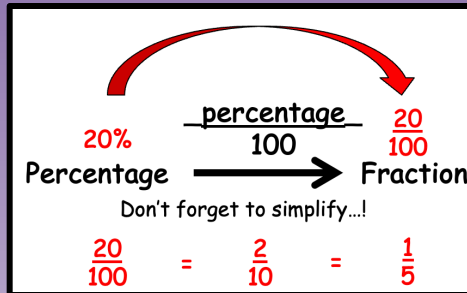
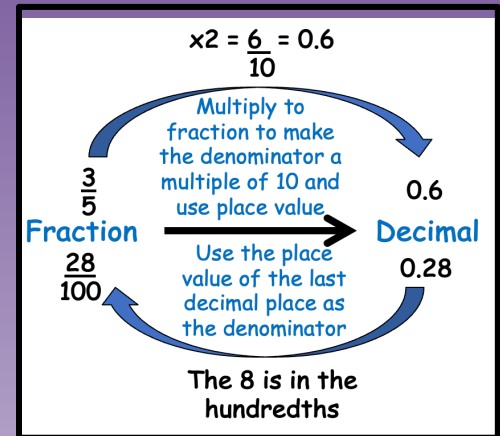
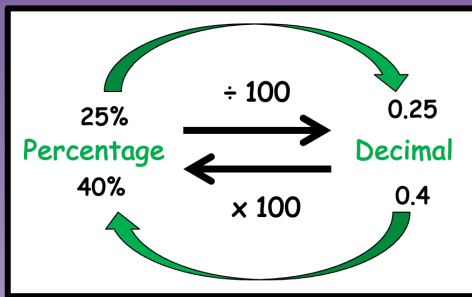
**Factorise  $20a^2 + 4a$**

The highest common factor of  $20a^2 + 4a$  is  $4a$

$5a + 1$  in brackets because when these are multiplied by  $4a$  you get your  $20a^2$  and  $4a$

So  $4a(5a + 1)$  is answer

# Chapter 4 - FDP



## Percentages

- An amount out of 100
- With a calculator:  
What is 40% of £50  
**Percentage  $\div 100 \times$  amount**
- Changing to a percentage:  
**Amount  $\div$  total  $\times 100$**
- Without a calculator:  
**1% = divide by 100**  
**10% = divide by 10**  
**25% = divide by 4**  
**50% = divide by 2**

## Fraction Arithmetic

**Multiplying** – Multiply top by top and bottom by bottom.

**Dividing** - 'Keep Change Flip'.

**Addition or Subtraction** – You need same bottom number (**denominator**). Add or subtract the numerator, keep the denominator the same.

## Recurring Decimals

A decimal with repeating values

We indicate the repeating numbers with a dot above

$$0.\dot{6} = 0.666666 \dots$$

$$0.\dot{6}\dot{5} = 0.656656656 \dots$$

## Improper and Mixed Fractions

Improper to mixed:

$$2\frac{3}{4} = \frac{(4 \times 2) + 3}{4} = \frac{11}{4}$$

Mixed fractions to improper

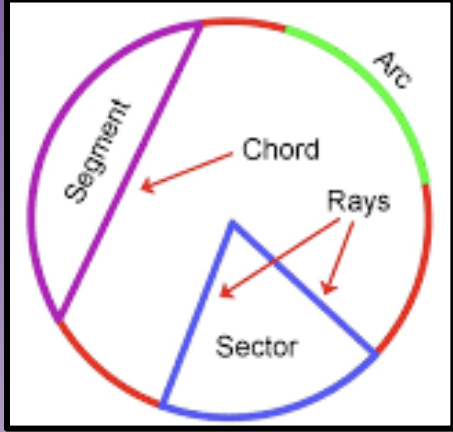
$$\frac{5}{3} = 5 \div 3 = 1 \text{ R}2$$

$$1\frac{2}{3}$$

# Chapter 5 – Angles and 2D Shapes

## Polygons

A shape with 3 or more straight sides  
 Total Interior Angles =  $(n-2) \times 180$   
 Interior + Exterior =  $180^\circ$   
 Sum of Exterior =  $360^\circ$



<p><b>Square</b></p> <p>4 equal sides                      4 angles of <math>90^\circ</math>                      2 sets of parallel sides</p>	<p><b>Rectangle</b></p> <p>2 sets of equal sides                      4 angles of <math>90^\circ</math>                      2 sets of parallel sides</p>	<p><b>Rhombus</b></p> <p>4 equal sides                      2 pairs of equal angles                      2 sets of parallel sides</p>	<p><b>Parallelogram</b></p> <p>2 sets of equal sides                      2 pairs of equal angles                      2 sets of parallel sides</p>
<p><b>Trapezium</b></p> <p>1 set of parallel sides</p>	<p><b>Isosceles trapezium</b></p> <p>1 set of equal sides                      2 pairs of equal angles                      1 set of parallel sides</p>	<p><b>Kite</b></p> <p>2 sets of equal sides                      1 pair of equal angles                      No parallel sides</p>	<p><b>Arrowhead</b></p> <p>2 sets of equal sides                      1 pair of equal angles                      No parallel sides</p>

# Chapter 6 - Graphs

## Coordinates

Remember “along the corridor then up the stairs”  
X and y values should be written on the axes  
There are 4 quadrants

## Horizontal and Vertical Lines

- An equation in the form  $y =$  always gives a horizontal line.
- An equation in the form  $x =$  always gives a vertical line.

## Parallel lines

- Parallel lines have the same gradient

## Plotting Straight Lines

- When plotting a linear graph always plot at least three coordinates.
- First create a table of values
- Substitute in values to form coordinate points
- Plot the coordinates one at a time

# Chapter 8 - Statistics

## Mean, median, mode and range

You must be able to get measures from a list of values or values in a frequency table

**MEAN** = Total of values  $\div$  Number of values

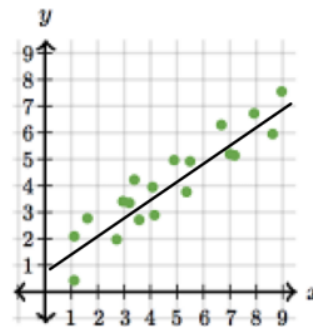
**MEDIAN** – The middle value when written in size order

**MODE** – The value that occurs the most often

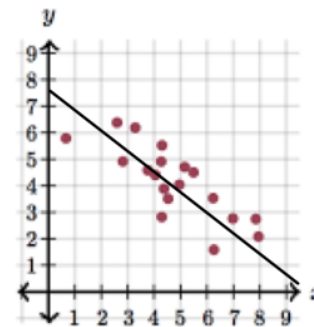
**RANGE** – Maximum value subtract minimum value

## Grouped data

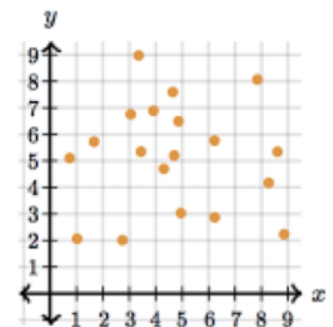
- As there is no original data, the mean is an estimate. Use the midpoint of each group.
- You can only find the modal class which is the group with the highest frequency.



Positive Correlation



Negative Correlation

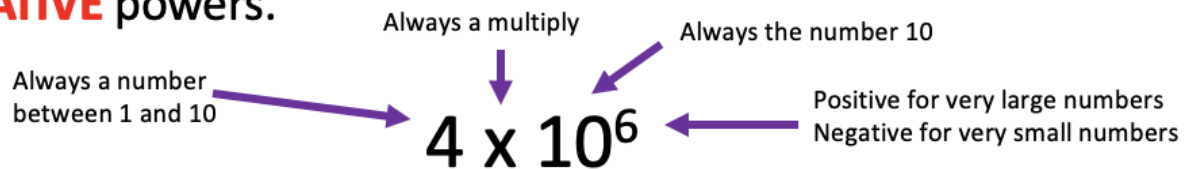


No Correlation

# Chapter 11 – Powers and Roots

## Standard Form

- A way of writing very **BIG** or very **SMALL** numbers
- Think **BIG** numbers – distance between planets and **SMALL** numbers – sizes of atoms.
- **BIG** numbers have **POSITIVE** powers and **SMALL** number have **NEGATIVE** powers.



## Powers

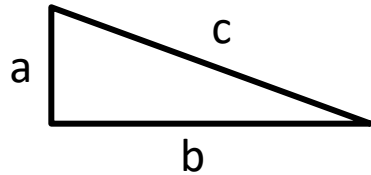
If we multiply powers we add.  $y^3 \times y^4 = y^{(3+4)} = y^7$

If we divide powers we subtract.  $y^{10} \div y^6 = y^{(10-6)} = y^4$

Anything to the power zero is always 1

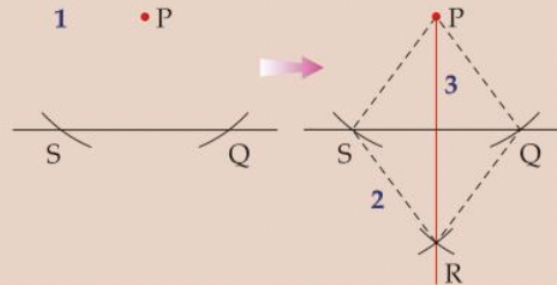
# Chapter 12 – Constructions and Triangles

## Pythagoras



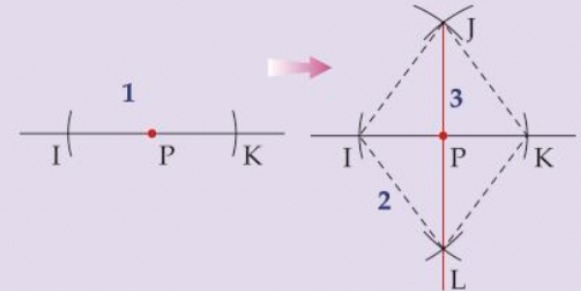
- $a^2 + b^2 = c^2$   
Square root  $c^2$  to find Hypotenuse
- $c^2 + a^2 = b^2$   
Square root  $b^2$  to find shorter side

### ▶ A perpendicular from a point to a line



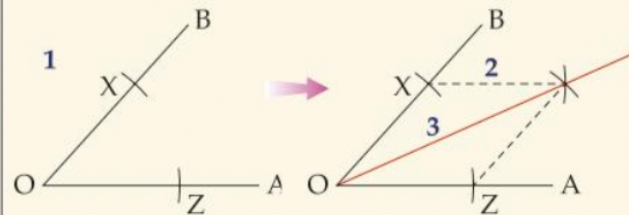
- 1 Draw arcs equidistant from P cutting the line at Q and S.
- 2 Using Q and S as centres, draw arcs below the line that cross at R.
- 3 Draw the line PR.

### ▶ A perpendicular from a point on a line



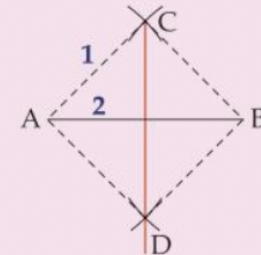
- 1 Draw arcs equidistant from P cutting the line at I and K.
- 2 Using I and K as centres, draw arcs above and below the line that cross at J and L.
- 3 Draw the line JL.

### ▶ An angle bisector



- 1 Draw arcs equidistant from O cutting OA and OB at Z and X.
- 2 Using X and Z as centres, draw arcs that cross at Y.
- 3 Draw the line OY.

### ▶ A perpendicular bisector of a line



- 1 Using A and B as centres, draw arcs above and below the line that cross at C and D.
- 2 Draw the line CD.

# Chapter 14 – 3D shapes and Trigonometry

## Right angled trig

- Identify Hypotenuse, Adjacent and Opposite
- Identify Sin, Cos or Tan function
- $\text{Sin}\theta = \frac{\text{opp}}{\text{hyp}}$
- $\text{Cos}\theta = \frac{\text{adj}}{\text{hyp}}$
- $\text{Tan}\theta = \frac{\text{opp}}{\text{adj}}$
- Use the normal function for sides
- Use the inverse function ( $\text{Sin}^{-1}$ ) etc for angles

## Terminology Shape

- Edge – Where 2 faces meet
- Vertices – Where 3 faces meet
- Face – side of a 3d shape
- Quadrilateral – a 4 sided polygon
- Polygon – a 2d shape with straight sides
- Acute – an angle less than  $90^\circ$
- Obtuse – an angle between  $90^\circ$  and  $180^\circ$
- Reflex – an angle more than  $180^\circ$

# Chapter 15 – Ratio and proportion

## Direct Proportionality

- Values that have a relationship with each other, as goes up so does the other at the same rate
- $Y = kx$
- $y$  is **directly proportional** to  $x$ .

Q: If  $y=24$ , then  $x=8$

Work out the value of  $y$  when  $x=2$ .

A:  $y = kx$   $24 = k \times 8$   $k=3$  and so  $y = 3x$

So when  $x = 2$   $y = 3 \times 2 = 6$

## Ratio as a measure

A ratio is a comparison of parts

Use a colon (:) to separate parts of a ratio

A colon is read as 'to'

2 or 3 parts

Understand the parts add up and stay in proportion

## Inverse Proportionality

- Values that have a relationship with each other, as one goes up the other goes down, at the same rate
- $y = \frac{k}{x}$
- $y$  is **inversely proportional** to  $x$ .

Q: When  $y=2$ ,  $x=3$ . Work out the value of  $y$  when  $x=18$

A:  $y = \frac{k}{x}$   $2 = \frac{k}{3}$   $k = 6$  and so  $y = \frac{6}{k}$

When  $x = 18$   $y = 6 \div 18 = 1/3$